Comparative Study of Alternative Energy Functions for the HP Model of Protein Structure Prediction

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Abstract—*Protein structure prediction is the problem of finding the functional conformation of proteins given only their amino acid sequence. The HP model is an abstract formulation of this problem, which captures the fact that hydrophobicity is the major driving force in the protein folding process. It represents a hard combinatorial optimization problem, widely addressed with metaheuristics. The conventional energy function of the HP model does not provide an effective discrimination among candidate solutions. Therefore, alternative energy formulations have been proposed. We inquire into the effectiveness of several of such alternative approaches. The discrimination potential of each of the studied functions is analyzed as well as their impact on the behavior of a basic local search algorithm.*

1. Introduction

Proteins are at the heart of cellular function, carrying most of the key processes associated with life. The functional properties of a protein are dictated by its three-dimensional conformation. To fully understand the biological roles of a protein it is imperative, therefore, to determine its structure.

The *Protein Structure Prediction* (PSP) problem aims to determine the native conformation of proteins given only their linear chain of amino acids. Such a structure is assumed to be the one minimizing the overall free energy [1]. Solving PSP at atomic resolution requires a prohibitive computational effort even for relatively small proteins. Thus, simplified protein models have emerged as valuable tools for studying the most general principles of the folding process.

One of such simplified formulations of PSP is the HP model [2, 3]. However, even a so abstract model represents a hard combinatorial optimization problem which has been proved to be $\mathcal{NP}$-complete [4, 5]. This has widely motivated the use of metaheuristics to address this problem [6].

Metaheuristics rely on an effective evaluation scheme to guide the search process. However, the conventional energy function of the HP model enables a very poor discrimination. Thus, no preferences can be set among potential solutions, leading the search to be oriented almost at random. This problem is expected to have a major impact on the performance of local search algorithms. The low discrimination

of the conventional function produces large plateaus in the energy landscape, on which local search strategies could fail to detect a promising search direction [7].

Alternative HP energy functions have been proposed to improve the performance of search algorithms [7]–[12]. Nevertheless, there are no reported results on the advantages of using most of such approaches. In this paper, a comparative study is presented where seven different formulations of the HP energy function are considered. The discrimination potential of these approaches is first analyzed. Then, the effectiveness of each of the studied functions to guide the search process is evaluated. A basic local search algorithm was adopted for this sake.

This paper is organized as follows. The HP model is defined in Section 2. In Section 3, the studied approaches are described. Our experimental results are discussed in Section 4. Finally, Section 5 concludes.

2. The HP model

Amino acids, the building blocks of proteins, can be classified on the basis of their affinity for water. *Hydrophilic* or *polar* amino acids (P) are usually found at the outer surface of proteins. By interacting with the aqueous environment, these residues contribute to the solubility of the molecule. In contrast, *hydrophobic* or *nonpolar* residues (H) tend to pack on the inside of proteins, where they interact with one another to form a water-insoluble core. These properties of the amino acids represent, therefore, one of the major driving forces responsible for the folded state of proteins.

In the Hydrophobic-Polar (HP) model, proposed by Dill in 1985 [2, 3], proteins are represented as sequences of the form $S \in \{H, P\}^L$, where L denotes the number of amino acids. The subsets of H and P residues in S are here referred to as S_H and S_P, respectively. Valid conformations are modeled as *Self-Avoiding Walks* of the HP sequence S on a lattice. That is, 1) lattice nodes are labeled by the amino acids, 2) a lattice node can be assigned to at most one residue and 3) adjacent residues in S are also adjacent in the lattice. This study focuses on the two-dimensional square lattice.

By emulating hydrophobic interactions, the HP model aims to find a valid conformation where the number of H-H *topological contacts* (HHtc) is maximized. Two residues

$s_i, s_j \in S$ are said to form a topological contact, denoted by $tc(s_i, s_j)$, if they are nonconsecutive in S (*i.e.*, $|i - j| \geq 2$) but adjacent in the lattice. The free-energy function in the HP model is defined as the negative of HHtc; maximizing HHtc is equivalent to minimize such an energy function.

Formally, PSP in the HP model is defined as the problem of finding the conformation $c^* \in C(S)$ such that $E_{D85}(c^*) = \min\{E_{D85}(c) \mid c \in C(S)\}$, where $C(S)$ is the set of all valid conformations of S. $E_{D85}(c)$ denotes the free energy of conformation c, which is given by:[1]

$$E_{D85}(c) = \sum_{s_i, s_j \in S_H} e(s_i, s_j) \qquad (1)$$

where

$$e(s_i, s_j) = \begin{cases} -1 & \text{if } tc(s_i, s_j) \\ 0 & \text{otherwise} \end{cases}$$

An example of the optimal conformation for an HP protein of length $L = 20$ on the square lattice is shown in Figure 1.
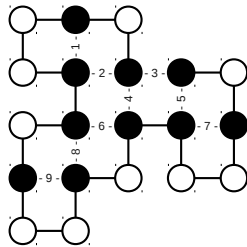

Fig. 1: Optimal conformation for sequence HPHPPHHPH-PPHPHHPPHPH of length $L = 20$. Black and white balls denote H and P residues, respectively. H-H topological contacts (HHtc) have been numbered. The free energy of this conformation is $E_{D85}(c) = -9$, since HHtc $= 9$.

Despite its apparent simplicity, finding the optimal conformation for a protein in the HP model is a hard combinatorial optimization problem, proved to be $\mathcal{NP}$-complete [4, 5].

3. Alternative HP energy functions

This section describes the alternative HP energy functions considered for this study. A three-letter acronym has been assigned to each of the studied approaches. The acronyms are based on first author's initial and publication year.

3.1 Krasnogor et al., 1999 (K99)

In the conventional HP energy function, only H-H topological contacts (HHtc) contribute to the quality assessment of conformations. Given two conformations with the same HHtc value, it is possible, however, that one of them has better characteristics (more compact) than the other. Krasnogor

et al. [7] proposed the following distance-dependent energy function:

$$E_{K99}(c) = \sum_{s_i, s_j \in S_H} e(s_i, s_j) \qquad (2)$$

where

$$e(s_i, s_j) = \begin{cases} -1 & \text{if } tc(s_i, s_j) \\ -1/(d(s_i, s_j)^k |S_H|) & \text{otherwise} \end{cases}$$

where $d(s_i, s_j)$ denotes the distance between residues s_i and s_j. In [7], the value of $k = 4$ was used for the square lattice.

In [7], no significant improvements were achieved when using the modified energy function. As the authors pointed out, the superiority of the approach is expected to become more evident for larger instances and, particularly, when local search strategies are implemented. The relevance of using this proposal needs to be further investigated.

3.2 Custódio et al., 2004 (C04)

The conventional HP energy function maximizes only H-H interactions, thus the positioning of P residues is not directly optimized. This may result in unnatural structures for sequences with long P segments and, especially, when P segments are located at the ends of the chain.

Custódio *et al.* [8] proposed a modified energy function based on the assumption that it may be preferable for an H residue to have a P neighbor than to be in contact with the aqueous solvent. In the proposed function, the energy of a conformation is computed as the weighted sum of the number of hydrophobic-hydrophobic (HHc), hydrophobic-polar (HPc) and hydrophobic-solvent contacts (HSc).[2] Formally:

$$E_{C04}(c) = \omega_1 HHc + \omega_2 HPc + \omega_3 HSc \qquad (3)$$

where ω_1, ω_2 and ω_3 denote the relative importance of HHc, HPc and HSc.

In [8], the proposed function allowed to improve the performance of a genetic algorithm for some of the adopted test cases.

3.3 Lopes and Scapin, 2006 (L06)

Lopes and Scapin [9] proposed an energy function which is based on the concept of *radius of gyration*. The radius of gyration is a measure of the compactness of conformations; the more compact the conformation, the smaller the value for this measure. The proposed function is given by:

$$E_{L06}(c) = HnLB \cdot RadiusH \cdot RadiusP \qquad (4)$$

The $HnLB$ term comprises the number of H-H topological contacts (HHtc) and a penalty factor which accounts for the violation of the self-avoiding constraint. Formally:

$$HnLB = \text{HHtc} - (NC \cdot PW) \qquad (5)$$

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[1]The acronym D85 is used to distinguish this conventional function from the other approaches considered in this study.

[2]A free lattice location is said to be occupied by the solvent.

where NC is the number of collisions and the penalty weight PW can be computed as $PW = (0.033 \cdot L) + 1.33$ [13].

Before defining the $RadiusH$ and $RadiusP$ terms, let us first define RgH as the radius of gyration for H residues:

$$RgH \quad = \quad \sqrt{\frac{\sum\limits_{s \in S_H} \left[(x_s - \bar{X})^2 + (y_s - \bar{Y})^2\right]}{|S_H|}} \quad (6)$$

where x_s and y_s are the coordinates of residue s while $\bar{X}$ and $\bar{Y}$ denote the mean coordinates for H residues. Analogously, we can compute RgP, the radius of gyration for P residues, by considering only P rather than H residues in (6).

The $RadiusH$ term measures how compact the hydrophobic core of the conformation is. This term is given by:

$$RadiusH \quad = \quad MaxRgH - RgH \quad (7)$$

where $MaxRgH$ is the radius of gyration of a totally unfolded conformation; *i.e.*, the maximum possible RgH value.

Finally, the $RadiusP$ term aims to push P residues away from the hydrophobic core. Given the previously defined RgH and RgP measures, the $RadiusP$ term is computed as:

$$RadiusP = \begin{cases} 1 & \text{if } (RgP - RgH) \geq 0 \\ \frac{1}{1-(RgP-RgH)} & \text{otherwise} \end{cases} \quad (8)$$

$RadiusP$ lies in the range $[0, 1]$. A value of $(RgP - RgH) > 0$ means that P residues are more exposed than H residues. This is a convenient scenario, so the $RadiusP$ term has no contribution to the final energy value ($RadiusP = 1$). Otherwise, $(RgP - RgH) < 0$ suggests H residues to be more spread than the P ones, so the energy value of the conformation is decreased. Note that (4) is to be maximized.

In [9, 13], no results are provided on the impact of using this function rather than the conventional approach.

3.4 Berenboym and Avigal, 2008 (B08)

Berenboym and Avigal [10] proposed an alternative energy function, called by them the *global energy*. In this function, each pair of nonconsecutive H residues contributes to the energy value, even if they are not topological neighbors:

$$E_{B08}(c) \quad = \quad \sum_{s_i, s_j \in S_H} e(s_i, s_j) \quad (9)$$

where

$$e(s_i, s_j) \quad = \quad \begin{cases} \frac{-1}{(x_{s_i}-x_{s_j})^2+(y_{s_i}-y_{s_j})^2} & \text{if } |i-j| \geq 2 \\ 0 & \text{otherwise} \end{cases}$$

In [10], the effects of using a local search operator within a genetic algorithm were investigated for both, the conventional and the proposed energy functions. However, an explicit comparison to demonstrate the advantages of using a particular energy function was not reported.

3.5 Cébrian et al., 2008 (C08)

Cébrian *et al.* [11] proposed an alternative formulation of the HP energy function which measures the deviation from the unit distance (*i.e.*, topological contact distance) for each pair of H residues. Let $d(s_i, s_j)^2 = (x_{s_i} - x_{s_j})^2 + (y_{s_i} - y_{s_j})^2$ be the distance between residues s_i and s_j, and let $dv(s_i, s_j) = d(s_i, s_j)^2 - 1$ denote its deviation from the unit distance. The energy value of a conformation c is given by:

$$E_{C08}(c) \quad = \quad \sum_{s_i, s_j \in S_H} dv(s_i, s_j)^k \quad (10)$$

where $k \geq 1$ is a parameter of the function, whose larger values give more weight to unit distances. We used $k = 2$, since this value seems to provide the best behavior based on the results reported in [11]. $E_{C08}(c^*) = 0$ would refer to the ideal (potentially unrealistic) scenario where all pairs of H residues are at a unit distance in conformation c^*. In [11], no experimental results were reported about the benefits of using the proposed energy function instead of the conventional one.

3.6 Islam and Chetty, 2009 (I09)

Islam and Chetty [12] proposed a modified HP function based on two measures: *H-compliance* and *P-compliance*.

H-compliance measures the proximity of H residues to the center of a hypothetical rectangle enclosing all H residues, denoted by the reference point (x_r, y_r). Formally:

$$H\text{-}comp(c) \quad = \quad \frac{\sum\limits_{s \in S_H} (x_r - x_s)^2 + (y_r - y_s)^2}{|S_H|} \quad (11)$$

where x_s and y_s denote the lattice coordinates of the s residue.

P-compliance is a measure of how close P residues are to the boundaries of a hypothetical rectangle enclosing all P residues, defined by x_{min}, x_{max}, y_{min} and y_{max}. Formally:

$$P\text{-}comp(c) = \frac{\sum\limits_{s \in S_P} \min \left\{ \begin{array}{l} |x_{min} - x_s|, |x_{max} - x_s|, \\ |y_{min} - y_s|, |y_{max} - y_s| \end{array} \right\}}{|S_P|} \quad (12)$$

Finally, the energy of a given conformation c is defined as:

$$E_{I09}(c) = \alpha E_{D85}(c) + H\text{-}comp(c) + P\text{-}comp(c) \quad (13)$$

where $E_{D85}(c)$ is the conventional HP energy function (see Section 2) and α is a high value integer constant to ensure this will be the dominant term in (13). We used $\alpha = 10,000$.

In [12], the advantages of using the proposed energy function were demonstrated for a 85-length HP benchmark sequence. However, the impact of using this function should be carefully investigated for a larger set of test cases.

4. Experimental Results

In this section, we investigate the effectiveness of the studied approaches. Note, however, that even when an alternative evaluation function is used, the goal of the optimization process remains to maximize HHtc, which is the singular objective in the HP model. In this study, the exclusive purpose for using alternative energy functions is to guide the search process in a more effective manner. Table 1 presents the 9 HP benchmark sequences adopted for this study.

Table 1: Benchmarks, length (L) and optimal value (HHtc*).

	Sequence	L	HHtc*
S1	HPHP$_2$H$_2$PHP$_2$HPH$_2$P$_2$HPH	20	9
S2	P$_2$HP$_2$H$_2$P$_4$H$_2$P$_4$H$_2$P$_4$H$_2$	25	8
S3	P$_3$H$_2$P$_2$H$_2$P$_5$H$_7$P$_2$H$_2$P$_4$H$_2$P$_2$HP$_2$	36	14
S4	P$_2$HP$_2$H$_2$P$_2$H$_2$P$_5$H$_{10}$P$_6$H$_2$P$_2$H$_2$P$_2$HP$_2$H$_5$	48	23
S5	H$_2$(PH)$_4$H$_3$P(HP$_3$)$_3$(P$_3$H)$_3$PH$_4$(PH)$_4$H	50	21
S6	P$_2$H$_3$PH$_8$P$_3$H$_{10}$PHP$_3$H$_{12}$P$_4$H$_6$PH$_2$PHP	60	36
S7	H$_{12}$PHPH(P$_2$H$_2$P$_2$H$_2$P$_2$H)$_3$PHPH$_{12}$	64	42
S8	H$_4$P$_4$H$_{12}$P$_6$(H$_{12}$P$_3$)$_3$HP$_2$H$_2$P$_2$H$_2$P$_2$HPH	85	53
S9	P$_6$HPH$_2$P$_5$H$_3$PH$_5$PH$_2$P$_4$H$_2$P$_2$H$_2$PH$_5$P H$_{10}$PH$_2$PH$_7$P$_{11}$H$_7$P$_2$HPH$_3$P$_6$HPH$_2$	100	48

4.1 Degree of discrimination

The discrimination strategy directly impacts the performance of search algorithms. That is, if it is not possible to set preferences among solutions the search process will be guided practically at random.

The degree of discrimination that each of the studied functions provides is investigated. We analyzed the distribution of ranks that these approaches induce on a set of candidate solutions. A ranking expresses the relationship among a set of items according to a given property. In the context of this study, potential conformations are ranked according to their quality. The first rank is assigned to the best solution, the next rank to the second best solution, and so on. Solutions with the same quality will share the same rank.

We adopted the *relative entropy* (RE) measure proposed by Corne and Knowles [14]. Given a set of n ranked solutions (there are at most n ranks, and at least 1), the relative entropy of the distribution of ranks D is defined as:

$$\text{RE}(D) = \frac{\sum_r \frac{D(r)}{n} \log(\frac{D(r)}{n})}{\log(1/n)} \qquad (14)$$

where $D(r)$ denotes the number of solutions with rank r. $\text{RE}(D)$ tends to 1 as approaching to the ideal situation where each solution has a different rank (*i.e.*, the maximum possible discrimination). On the other hand, when all the solutions share the same ranking position (*i.e.*, the poorest discrimination), $\text{RE}(D)$ takes a value of zero.

In this experiment, $1,000$ different valid structures were generated at random. For each of the studied energy functions, these solutions were evaluated and ranked to finally compute the RE measure. We performed 100 repetitions of this experiment for all the benchmarks. The box plots in Figure 2 present the overall statistics of this experiment.
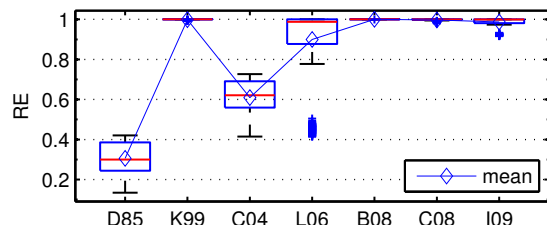

Fig. 2: Relative entropy (RE). Overall statistics.

From Figure 2, it is possible to note that the conventional HP function, D85, achieved the lowest RE values. This confirms the poor discrimination capabilities of this function, which has been the main factor motivating the exploration of alternative approaches. C04 showed the worst performance among the alternative functions. Function L06 achieved high RE values most of the time, but the outliers indicate a low performance of this function for some of the benchmarks. Finally, it is important to remark the high discrimination provided by functions B08, K99, C08 and I09.

The above results can be better understood by analyzing Figure 3. This figure presents the histograms with the distribution of ranks achieved by each function for the first repetition of this experiment regarding sequence S1. From this figure, it is possible to note how poor the distribution of ranks achieved by function D85 is. Only five different ranking positions were enough to classify the $1,000$ generated solutions. It can be seen a peak where there are almost 400 solutions sharing the same rank. In fact, no matter the amount of generated solutions, the maximum number of ranks which can be assigned through function D85 is 9, since HHtc$^* = 9$ for this benchmark sequence (S1). The second worst scenario is presented by function C04, where less than 40 different ranking positions were required, out of which two were each assigned to at around 100 conformations.

Functions L06 and I09 showed an increased discrimination, since about 720 and 650 ranking positions were occupied to classify the totality of solutions, respectively. In the case of function I09, a maximum of eight solutions were assigned to the same rank. On the other hand, the histogram for L06 presents a high peak indicating that there are about 250 equally ranked conformations. Function L06 is defined as the product of three terms, out of which one corresponds to HHtc (see Section 3.3). All solutions for which HHtc $= 0$ will have the same energy value, 0. To some extent, this can be seen as a drawback. Function L06 will not be able to discriminate among these solutions even if some of them have better chances than others to further improve.

Finally, the histograms for B08, K99 and C08 confirm the high degree of discrimination these approaches provide. We can see that function C08 allowed roughly 950 different ranks to be assigned. B08 showed the strongest discrimination among all the studied functions, followed by K99. The corresponding histograms for these functions reveal that almost all solutions were mapped to a different rank. Only a few ranks were assigned to at most two solutions.
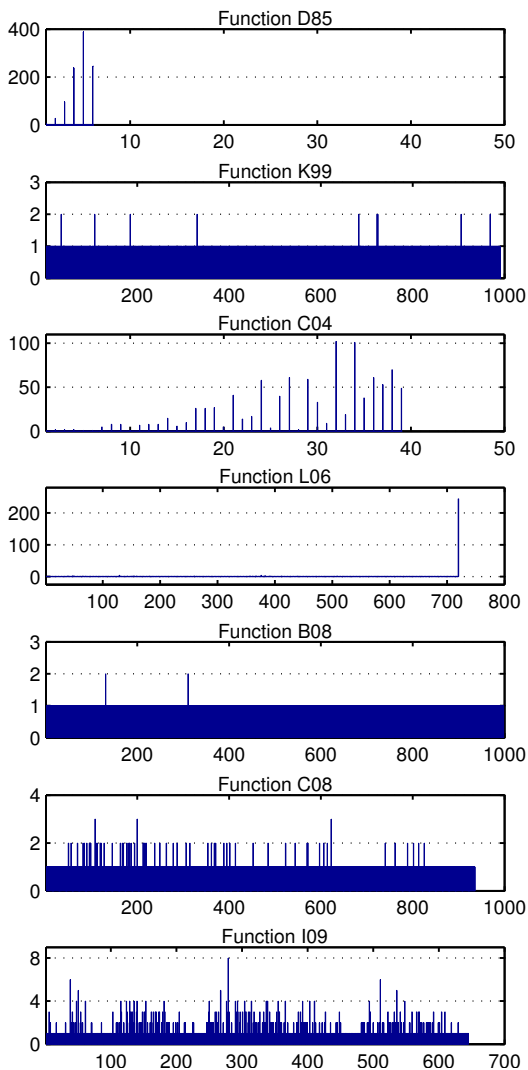
Fig. 3: Density of the distribution of ranks achieved by the studied evaluation functions. Sequence S1, run 1.

4.2 Search performance

We implemented a *Steepest Descent Hill Climbing* algorithm (SDHC) to evaluate the effectiveness of the studied energy functions at guiding the search process. SDHC is a parameter-free algorithm, whose motivation in this study is to avoid affecting (neither negatively nor positively) the performance of the approaches through parameter settings. Given that SDHC is a local search technique, functions providing a finer discrimination are expected to perform better. As pointed out by Krasnogor *et al.* [7], a poor discrimination will produce large plateaus in the energy landscape, on which local search strategies could fail to identify a descent direction. Algorithm 1 describes the implemented SDHC.

The algorithm starts with a valid conformation generated at random, denoted by c. Once c is generated, we identify c', the best conformation among all defined in the neighborhood of c, $N(c)$. Then, solutions c and c' are compared with respect to their energy values. At this point is where the

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Algorithm 1 Steepest Descent Hill Climbing (SDHC).

BEGIN SDHC()
1:   $c \leftarrow getRandomValidSolution()$
2:   **loop**
3:     $c' \leftarrow getBest(N(c))$
4:     **if** $E(c') < E(c)$ **then**
5:       $c \leftarrow c'$
6:     **else**
7:       $Stop()$
END

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different energy functions come to play a decisive role in the behavior of the algorithm. If c' has a better energy value than c ($E(c') < E(c)$), then a replacement occurs and the process repeats. Otherwise, the process ends, since given the current solution and the adopted neighborhood it is not possible to achieve an improvement (c is locally optimal).

An internal coordinates representation with absolute moves was adopted [15]. Candidate conformations are encoded as sequences in $\{U, D, L, R\}^{L-1}$, denoting the up, down, left and right possible locations for a residue with regard to the preceding one (solutions are decoded to Cartesian coordinates for evaluation). The implemented neighborhood structure $N(c)$ is defined by all solutions that can be reached through 1-variable perturbations of c. Given a sequence of length L, the size of such a neighborhood is $|N(c)| = 3(L-1)$. However, only valid conformations are considered.

It is important to remark that the aim of using the SDHC algorithm is not to improve the state-of-the-art results for this problem. In this study, SDHC serves only as a tool to measure the impact of using each of the energy functions.

The behavior of the SDHC algorithm was evaluated when using each of the studied functions. A total of 100 independent executions were performed for all the adopted benchmarks. The results of this experiment are presented in Figure 4. Each plot in this figure shows the average number of H-H topological contacts (HHtc) achieved by the algorithm as the search progressed (iteration by iteration).

From Figure 4, it is possible to derive some general conclusions. The poorest performance for this experiment was presented by function C08, whose results were even worse than those of function D85 in most of the considered test cases. This behavior can be explained by the fact that function C08 is not consistent with the conventional objective of the HP model. As stated at the beginning of Section 4, even when alternative functions are used to guide the search process, the goal remains to maximize HHtc; or, which is equivalent, to minimize function D85. The alternative function should not contradict D85 when discriminating among potential conformations, otherwise we will probably be pursuing a different optimum. Nevertheless, given two conformations c_1 and c_2, it is possible the case where $E_{D85}(c_1) < E_{D85}(c_2)$ but $E_{C08}(c_1) > E_{C08}(c_2)$,
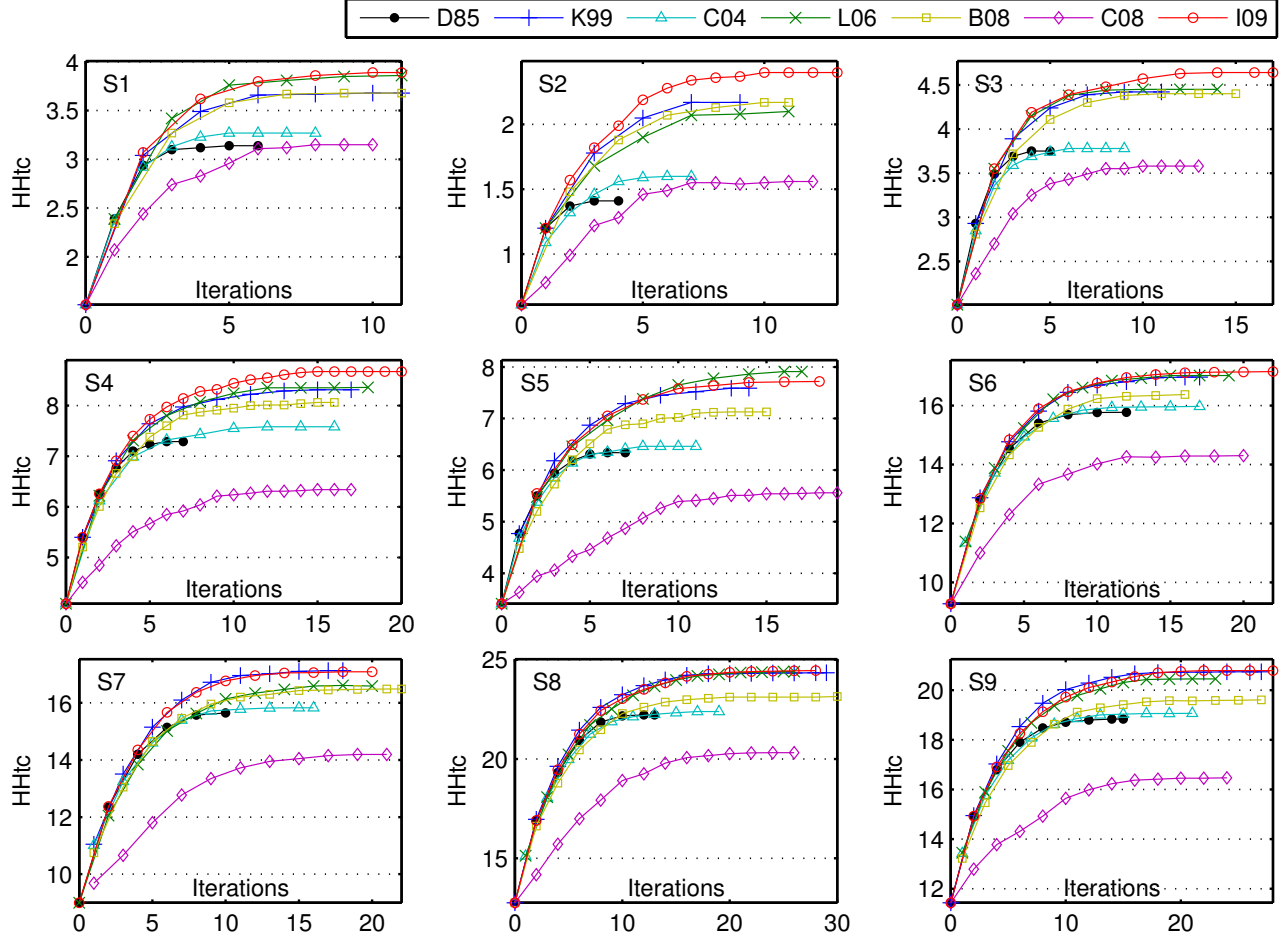
Fig. 4: Results of the SDHC algorithm. Achieved number of H-H topological contacts (HHtc) at each iteration. Average of 100 independent executions.

which is a contradiction.[3] An example of this scenario is presented in Figure 5. This can be seen as a drawback, so function C08 is not expected to steer the search in an effective manner. Such an important issue needs to be further explored for all the studied approaches.

c_1: $ULLDRDLDLLDDRURRURU$ c_2: $LUUULURRRDRDLLDRRRU$
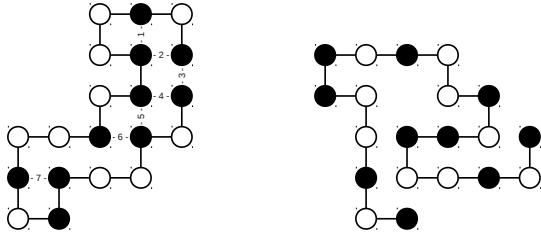

Fig. 5: C08 contradicts D85, since $E_{D85}(c_1) = -7 < E_{D85}(c_2) = 0$ but $E_{C08}(c_1) = 5548 > E_{C08}(c_2) = 5308$.

As expected, function D85 showed a low performance for

[3]Note that the case where $E_{D85}(c_1) = E_{D85}(c_2)$ but $E(c_1) \neq E(c_2)$ is not a contradiction. This is a convenient scenario, since the aim of using the alternative function E is to enable a more fine-grained discrimination.

this experiment. For all instances, the algorithm achieved the lowest number of iterations due to the poor discrimination this function provides. Function D85 exposed the second worst overall behavior. C04 reached slight improvements, but its limited performance was comparable with that of function D85 in some cases. Note that functions D85 and C04 were previously identified in Section 4.1 because of their low discrimination capabilities. To some extent, this explains the poor performance presented by these approaches.

Functions K99 and B08 behaved similarly for the smallest benchmarks, but their performance curves diverged as the size of the problem was increased. The results of B08 deteriorated for the largest test cases, while the increasing performance of K99 allowed this function to compete at the top of the ranking. L06 obtained very competitive results most of the time. Finally, we can highlight the outstanding behavior that function I09 consistently showed for all the considered test cases. Our results indicate that the best performers were I09, L06 and K99, in this order.

Functions I09, K99, B08 and C08 were all identified in Section 4.1 to provide a strong discrimination. However, only K99 and I09 are among the best performers of

this experiment. That some equally discriminative functions performed better than others suggests that more important than the strength is the effectiveness of the discrimination (intensity does not imply effectiveness).

5. Conclusions and Future Work

The conventional energy function of the HP model enables a very poor discrimination among potential conformations. Nevertheless, an effective evaluation scheme is an essential requirement for metaheuristics in order to guide the search process towards promising regions of the solutions space. Alternative HP energy functions have been proposed to enhance the performance of search algorithms. However, for most of these approaches there are not reported experimental results where the benefits of their usage are demonstrated.

This paper presented the results of a comparative study where seven different formulations of the HP energy function were considered. Our first experiment was concerned with the analysis of the degree of discrimination that each of these functions provides. The obtained results confirmed the poor discrimination capabilities of the conventional function, which has been the main motivation for exploring alternative approaches. All the alternative functions demonstrated to provide a more fine-grained discrimination. The most discriminative function according to our results is B08, followed by the K99, C08 and I09 approaches, in this order.

In our second experiment, we evaluated the impact of using the studied functions on the performance of a parameter-free local optimizer. The aim of using a parameter-free algorithm was to avoid influencing the behavior of the approaches through parameter settings. In general, most of the alternative functions allowed to increase the performance of the implemented algorithm. As expected, the conventional D85 function exhibited a low performance for this experiment. However, the C08 approach behaved even worse for most of the adopted test cases. On the other hand, functions I09, L06 and K99 consistently achieved very competitive results, being the best performers in this test.

From this study, it is possible to derive some general conclusions. First, intensity of discrimination does not necessarily imply effectiveness at guiding the search process. Even when functions I09, K99, B08 and C08 were all identified to provide a strong discrimination, only I09 and K99 behaved favorably. In contrast, B08 and particularly C08 presented a limited search performance. That the less discriminative approaches (D85 and C04) showed a low overall performance confirmed, however, that a tighter evaluation scheme is important to improve the behavior of search algorithms.

The fact that D85 consistently exposed a poor performance supports the relevance of exploring the use of alternative approaches. To the best of our knowledge, this research is producing the first results that have been reported in this direction. Nevertheless, this research is in progress. The preliminary results presented in this paper suggest that functions I09, L06 and K99 are very promising approaches for studies on the HP model. However, the impact of using these approaches needs to be further investigated for more sophisticated search algorithms. Also, it is important to extend this study to the three-dimensional cubic lattice, or to other lattice configurations (for example, the face-centered cubic lattice), in order to generalize our conclusions.

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